

Study of Gray Code Input DAC for Glitch Reduction



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Outline

- Research Objective
- Introduction to DAC
- Glitches
- Introduction to Gray Code
- Gray Code Input DAC
 - Switch Matrix Design
 - Voltage Mode Gray Code Input DAC
 - Current Steering Mode Gray Code Input DAC
- Conclusion

Research Objective

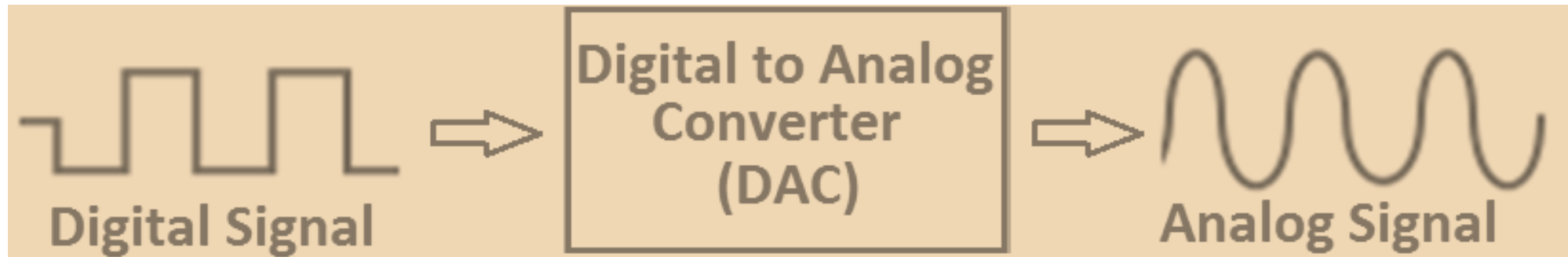
- ✓ Research and implement DAC for glitch reduction using Gray code input
*(difficult to design)

Approach

- ✓ Use MOSFETs for DAC design
- ✓ Utilization of Gray code input for glitch reduction

Introduction to DAC

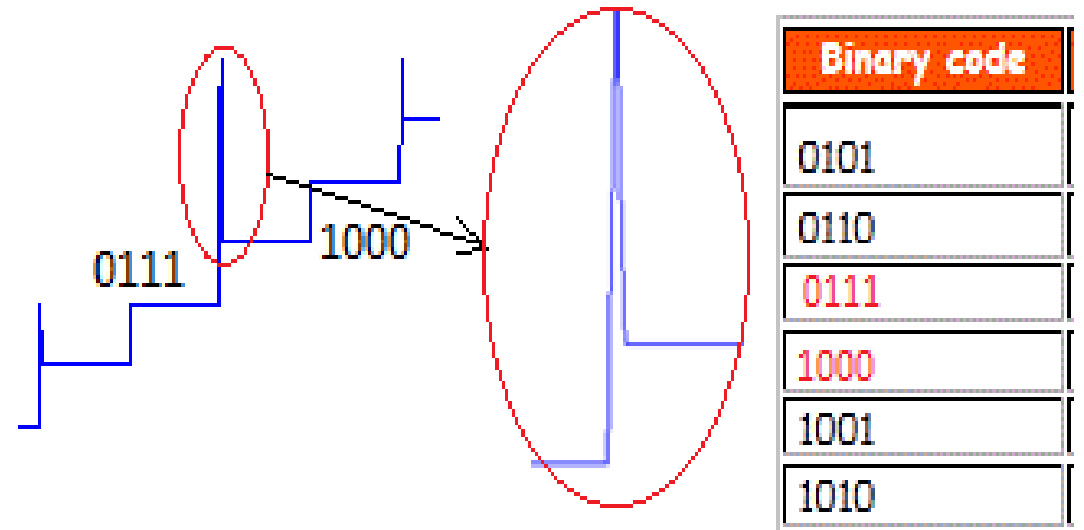
- Convert digital signal to analog signal



- Signal to be recognized by human senses
- Widely used in signal processing

What are Glitches ?

- ✓ Voltage spikes
- ✓ Reasons for glitches
 - Capacitive coupling
 - Differences in switching



- Glitch behaviour → Dominated by difference in switching
- Switching of MSB → Most significant glitches
(Multiple switches changing states at once)

Glitch Problem and Remedy

Effects of Glitch

- Serious deterioration of images, videos and sounds



Remedy

- Using high-order reconstruction filter
- Using track/hold circuitry at the DAC output

} ~~Extra Space in IC,
Expensive~~

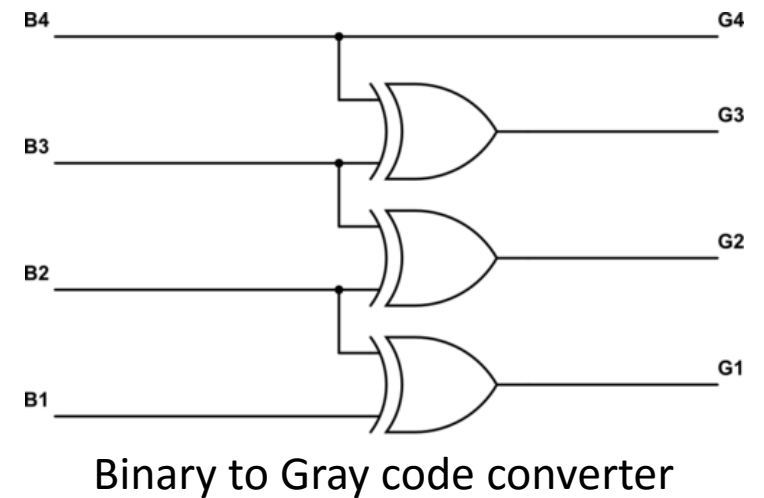
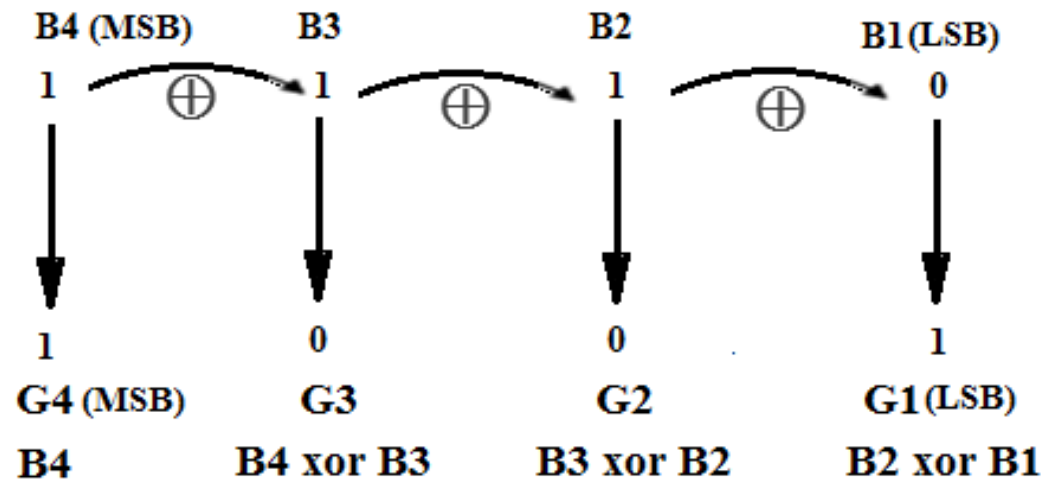
- **Using Gray code input DAC topologies**



What is Gray code ?

- Gray code → Alternative representation of binary code
- Two adjacent numbers → Only one bit change
- Reflected binary code

Binary to Gray code conversion



Gray Code versus Binary Code

Binary code Multiple bits change at a time



Trigger more switches

Example. 1 → 2 --- 00**01** → 00**10** 2 bits change

7 → 8 --- **0111** → **1000** all 4 bits change

Gray code Only one bit changes at a time



Triggers one switch

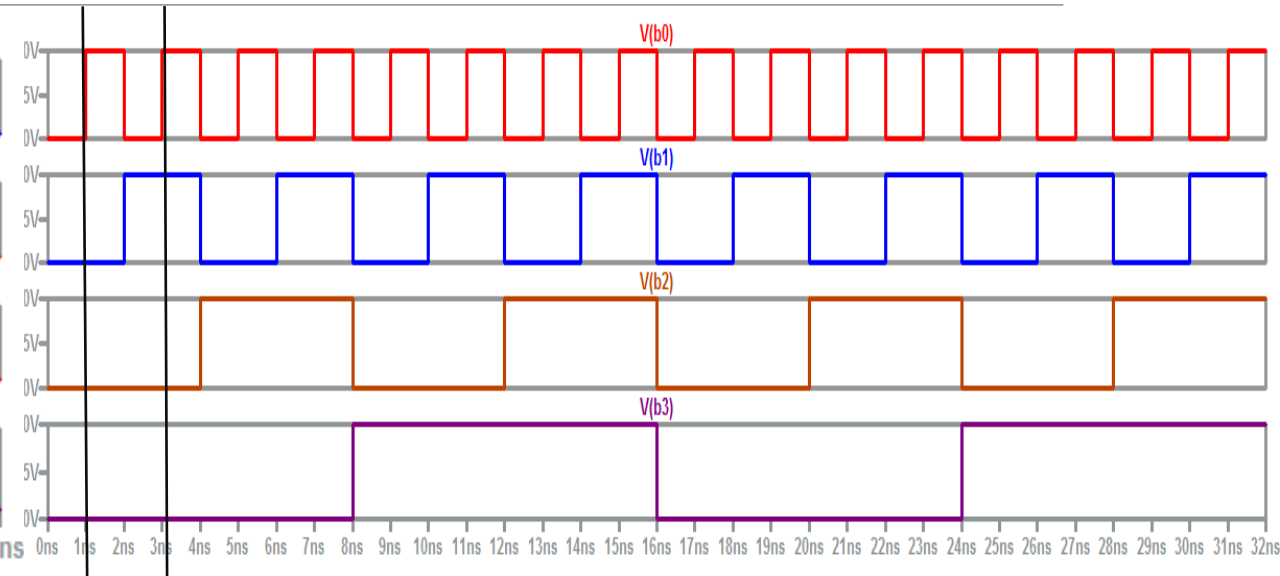
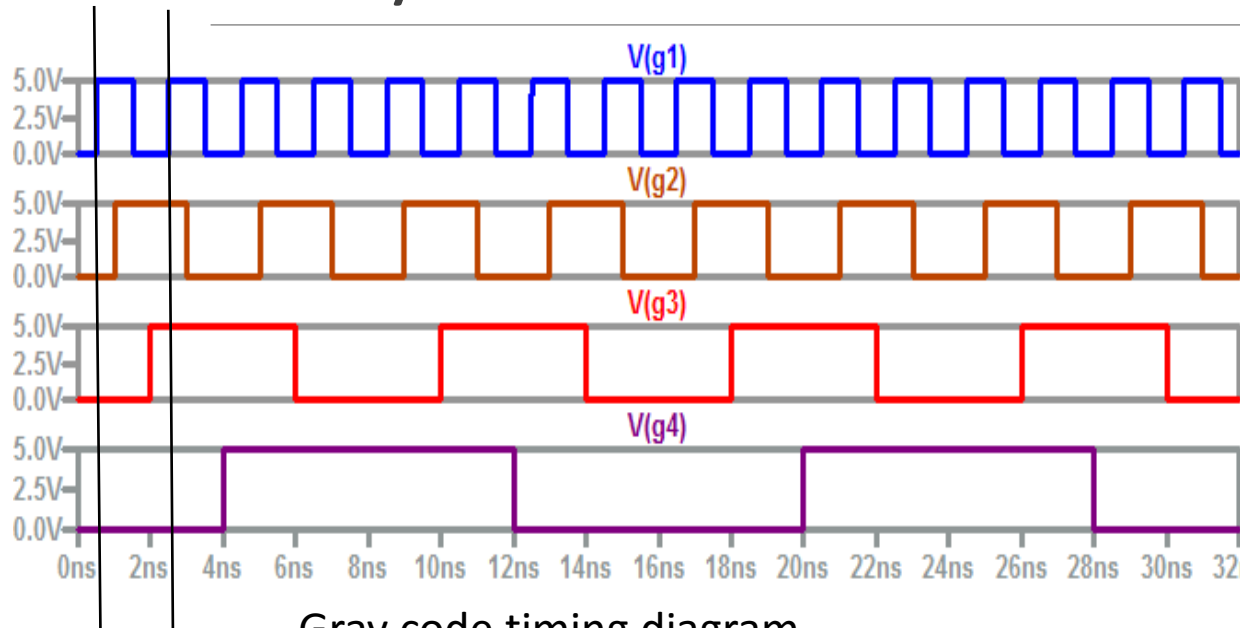
Example. 1 → 2 --- 00**01** → 00**11** one bit change (B2)

7 → 8 --- **0100** → **1100** one bit change (B4)

➡ Less glitches

Decimal	Binary	Gray
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101
10	1010	1111
11	1011	1110
12	1100	1010
13	1101	1011
14	1110	1001
15	1111	1000

Gray code versus Binary code Timing Diagram

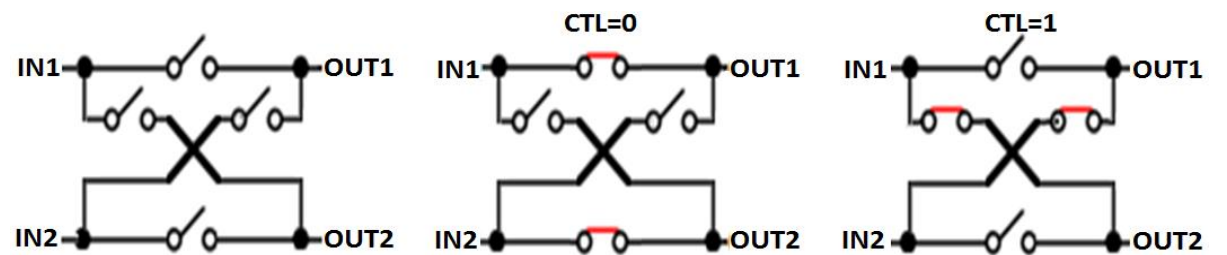
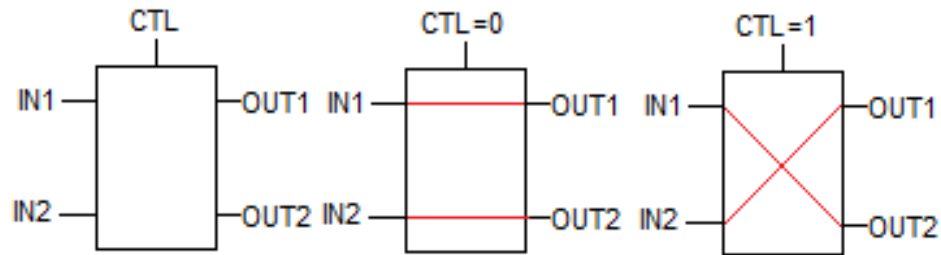


Gray code → Only one bit changes at a time 0001→0011
Binary code → Multiple bits change at a time 0001→0010

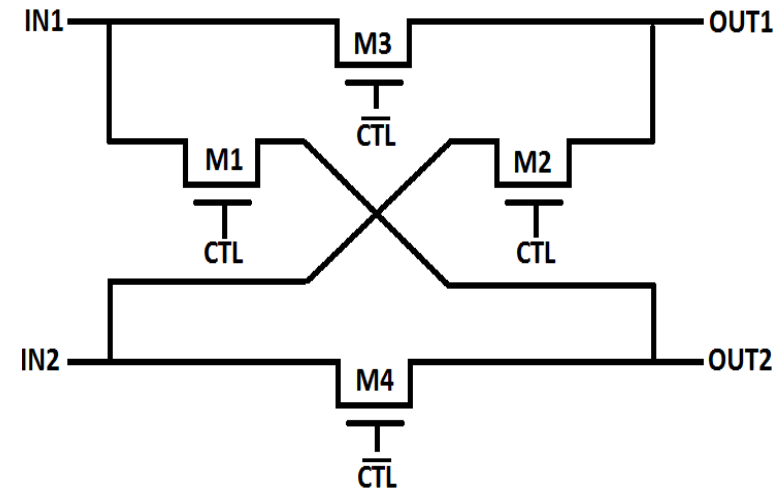
Using Gray code → Less glitches expected to appear

Gray Code Input DAC

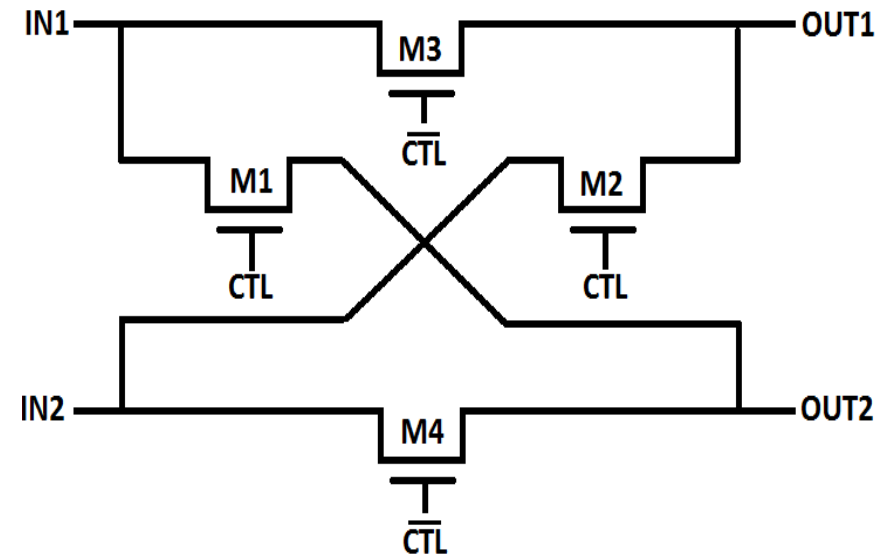
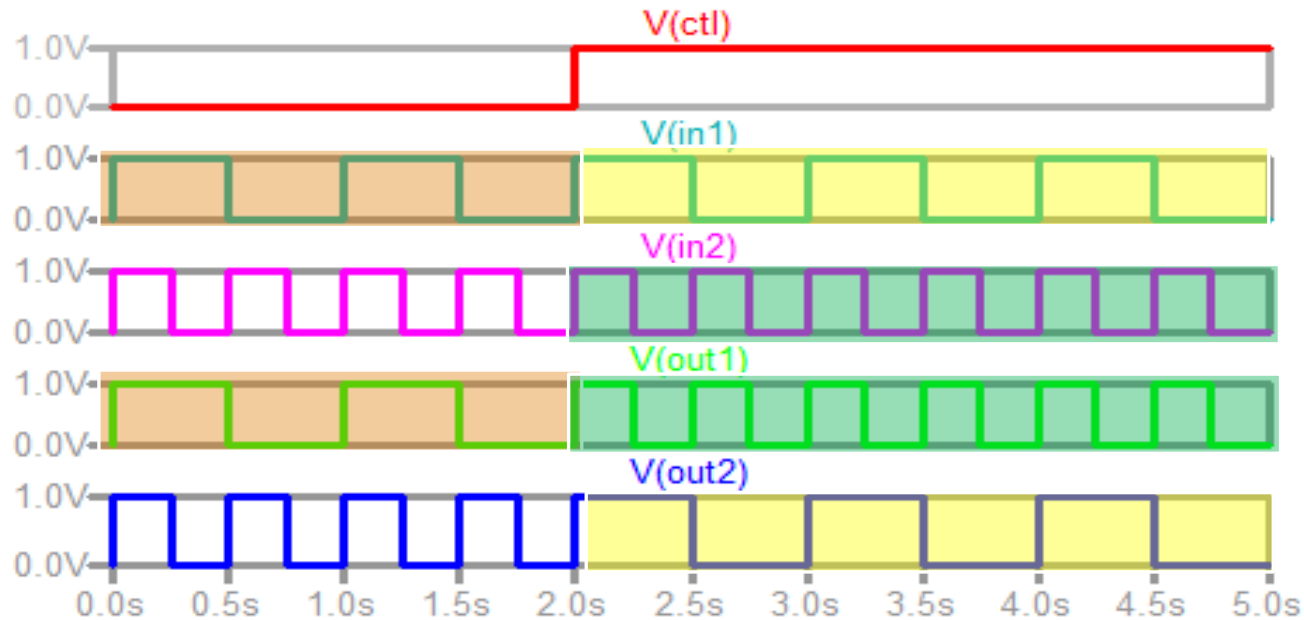
Switch Matrix Design



Switch is DPDT (Double-Pole Double-Throw)



Switch Matrix Operation



CTL → LOW:

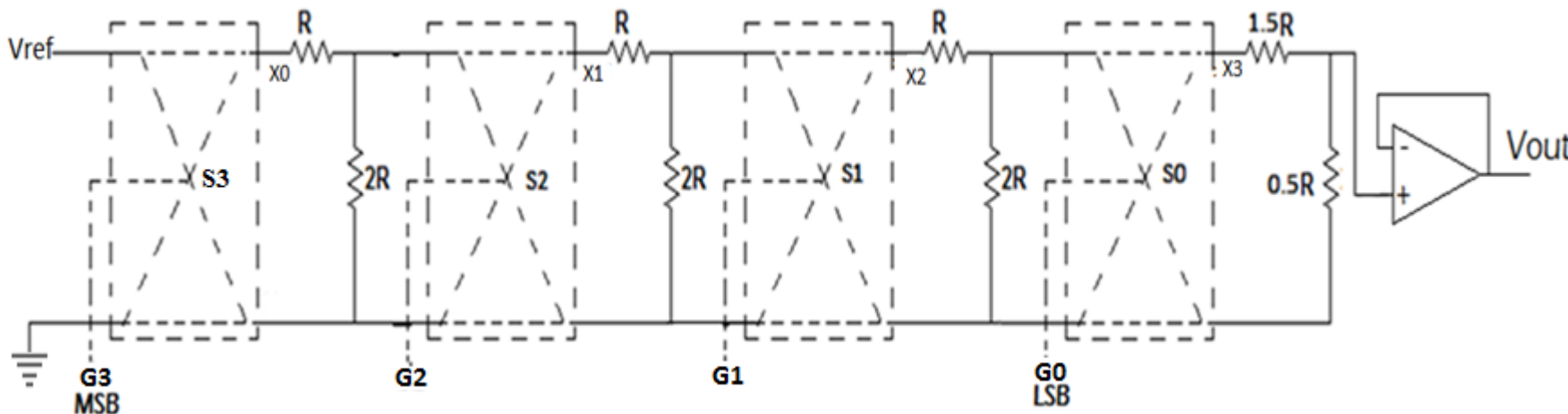
M3, M4 → ON, M1, M2 → OFF
 IN1 = OUT1, IN2 = OUT2

CTL → HIGH:

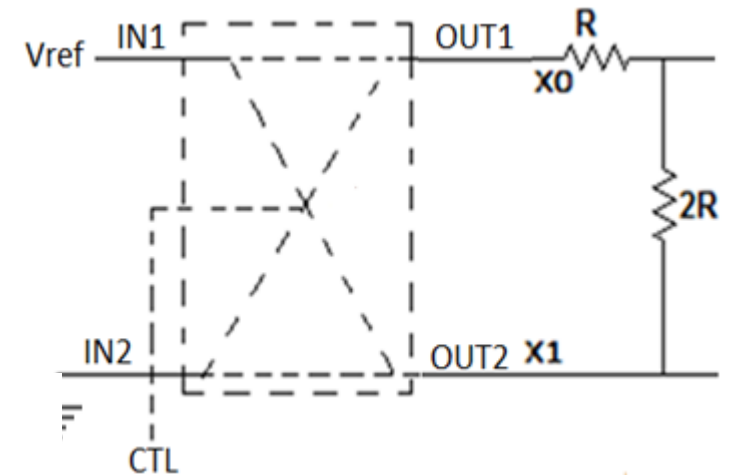
M1, M2 → ON, M3, M4 → OFF
 IN1 = OUT2, IN2 = OUT1

Voltage Mode Gray Code Input DAC

- IN1 = Vref
- IN2 = 0
- CTL ← Gray code input
- OUT1, OUT2 → Connected with R-2R Ladder



- Final stage → terminated with 1.5R, 0.5R resistors.



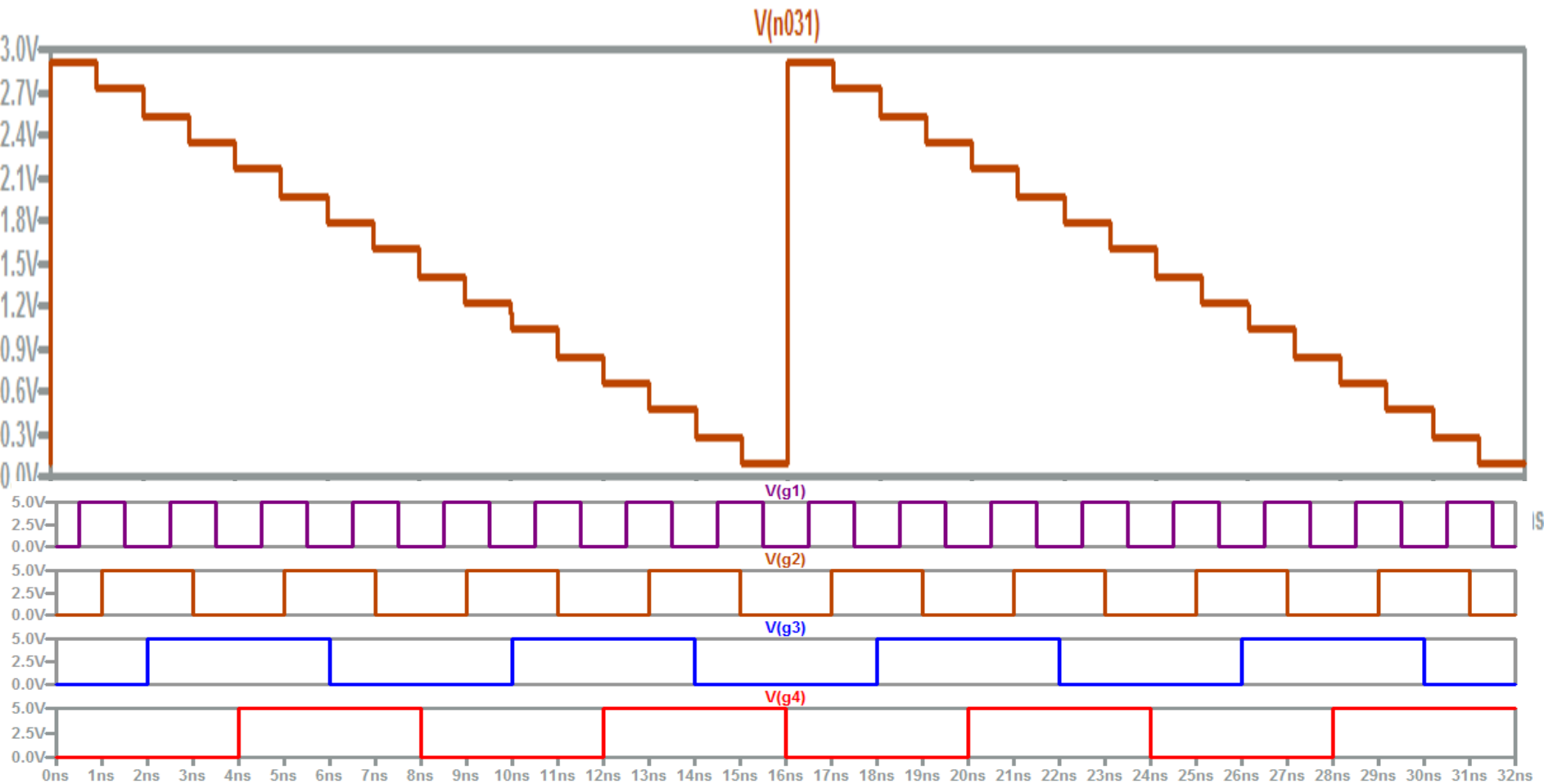
$$V_{out}(D) = \frac{V_{ref}}{2^{n+1}} |(2D - 1)|$$

n : number of bits
D = 1, 2, 3...n+1

Voltage Mode Gray Code Input DAC

SPICE Simulation Results

4-bit case

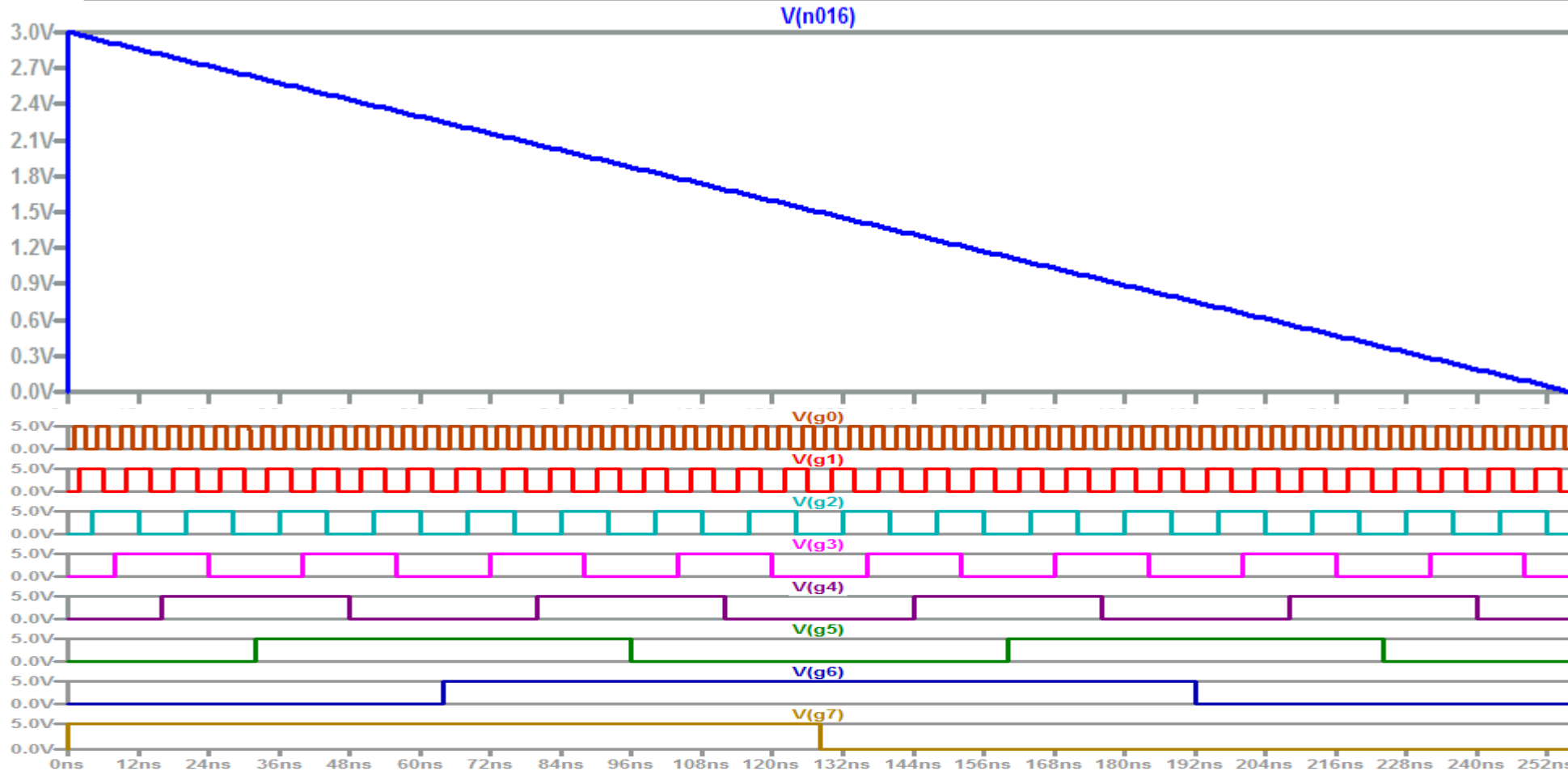


D	Bits	Vout	
1	0000	3/32	0.09375
2	0001	9/32	0.28125
3	0011	15/32	0.46875
4	0010	21/32	0.65625
5	0110	27/32	0.84375
6	0111	33/32	1.03125
7	0101	39/32	1.21875
8	0100	45/32	1.40625
9	1100	51/32	1.59375
10	1101	57/32	1.78125
11	1111	63/32	1.96875
12	1110	69/32	2.15625
13	1010	75/32	2.34375
14	1011	81/32	2.53125
15	1001	87/32	2.71875
16	1000	93/32	2.90625

Voltage Mode Gray Code Input DAC

8-bit case

SPICE Simulation Results



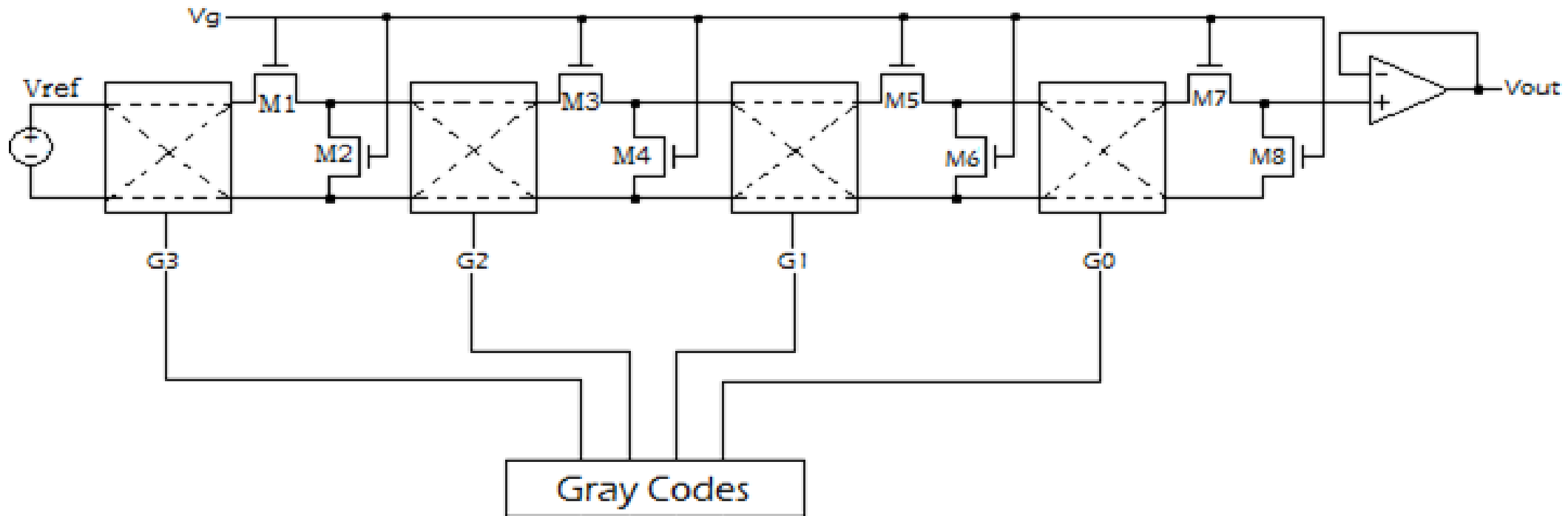
NO GLITCHES



Voltage Mode Gray Code Input DAC MOSFET Implementation

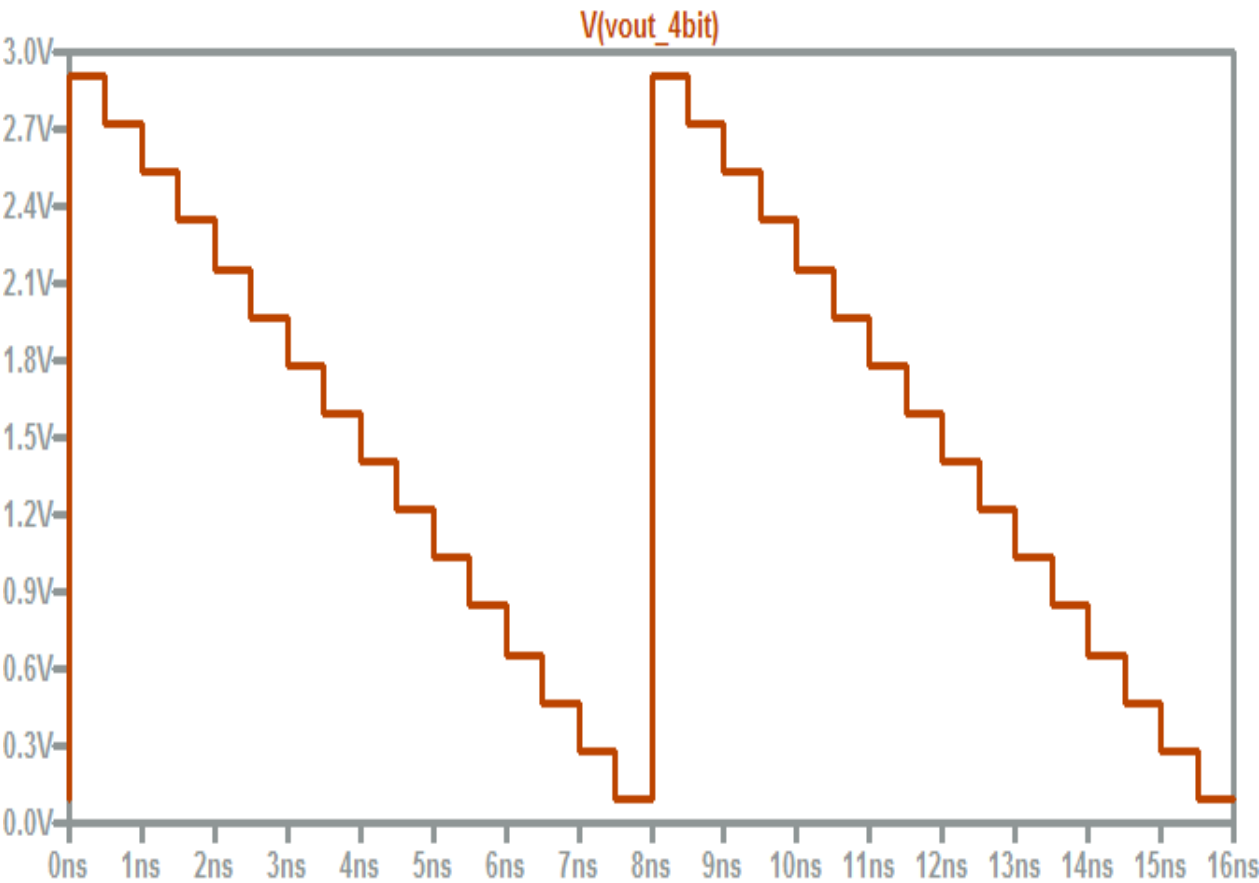
Aspect ratios W/L for R, 2R, 1.5R, 0.5R

$$R = \frac{V_{DS}}{I_{dsat}} = \frac{V_{DS}}{\frac{\mu_n C_{ox}}{2} \times \left(\frac{W}{L}\right) \times (V_{GS} - V_{TH})^2}$$

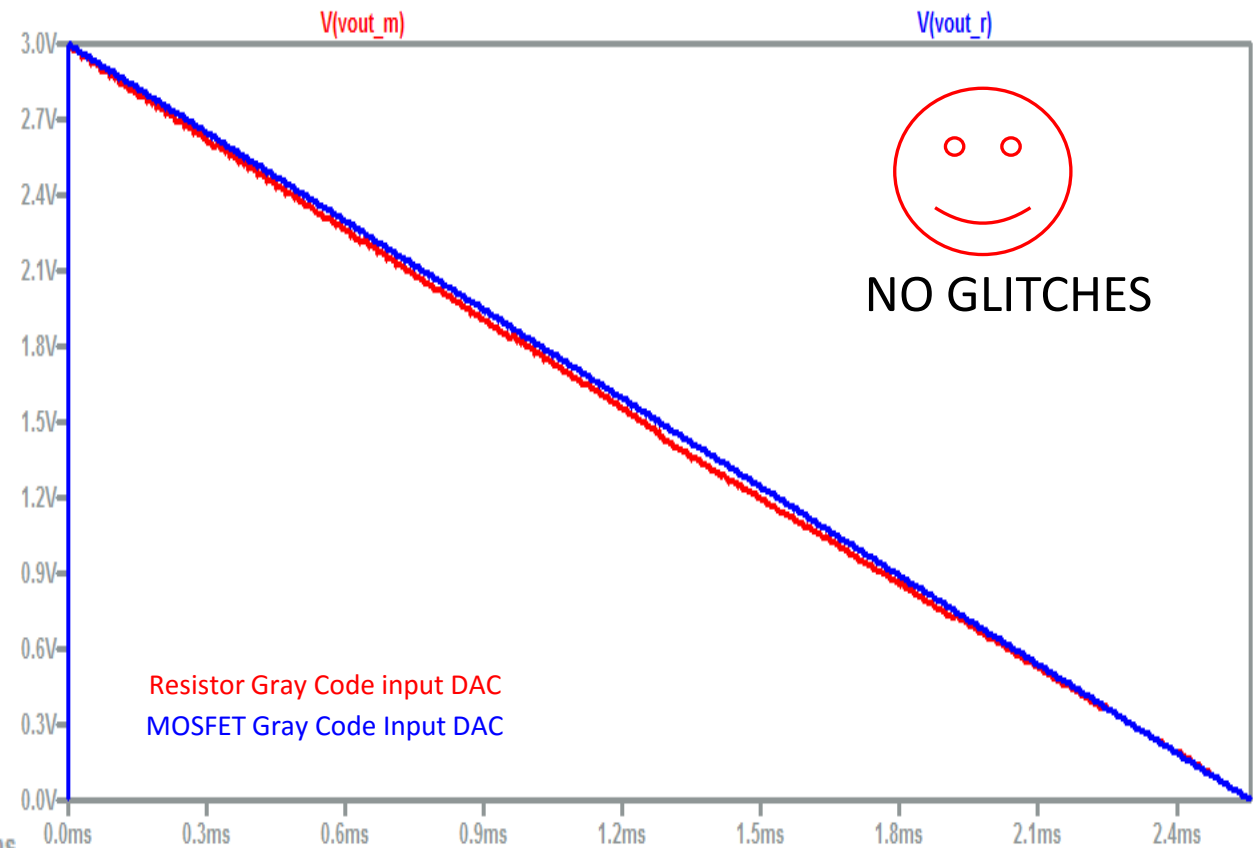


Voltage Mode Gray Code Input DAC MOSFET Implementation Simulation Results

4-bit case

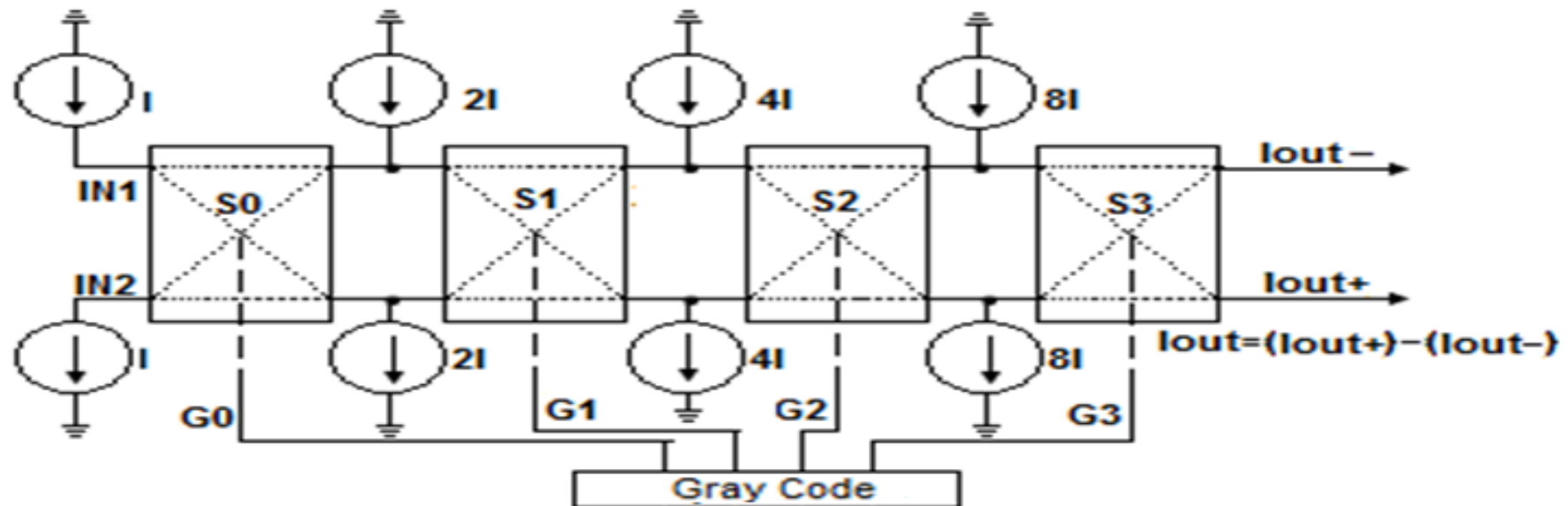


8-bit case



Current Steering Mode Gray Code Input DAC Circuit Configuration

- IN1, IN2, intermediate stages → binary weighted current sources.
- Gray code alters the way the switches are triggered
- $I_{out} = I_{out+} - I_{out-}$



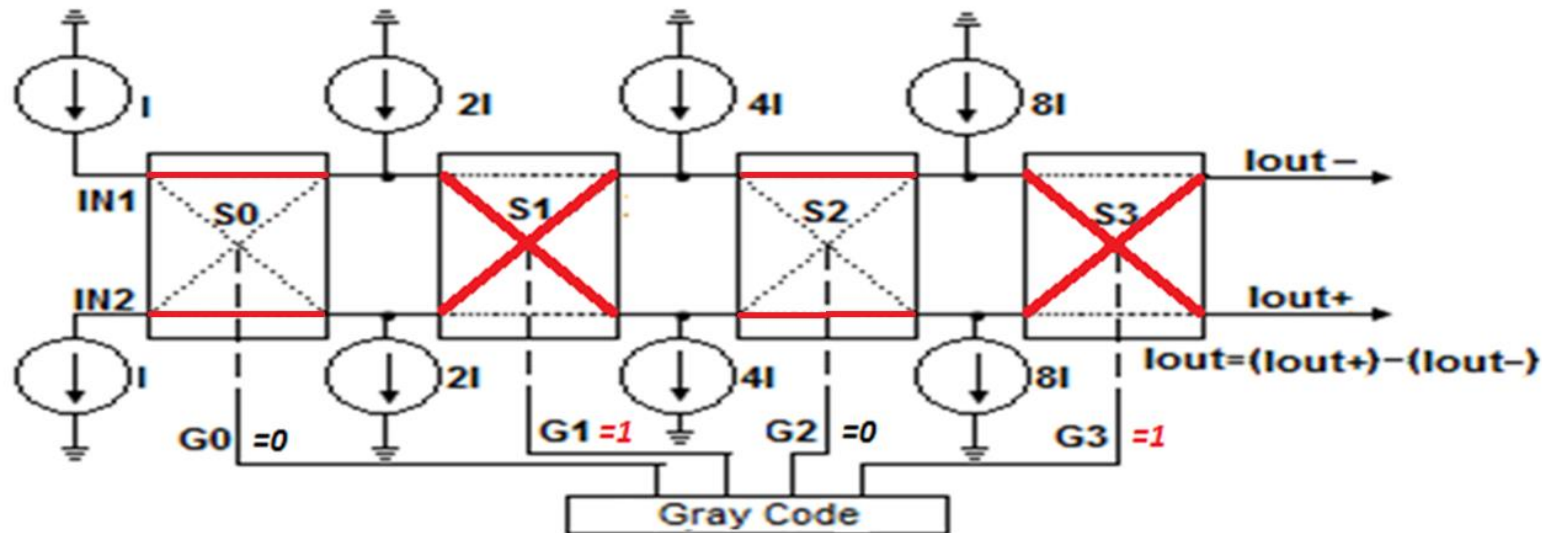
Current Steering Mode Gray Code Input DAC Circuit Operation

For 1010 Gray code,

$S_3, S_1 \rightarrow \text{ON}$, the other switches $\rightarrow \text{OFF}$

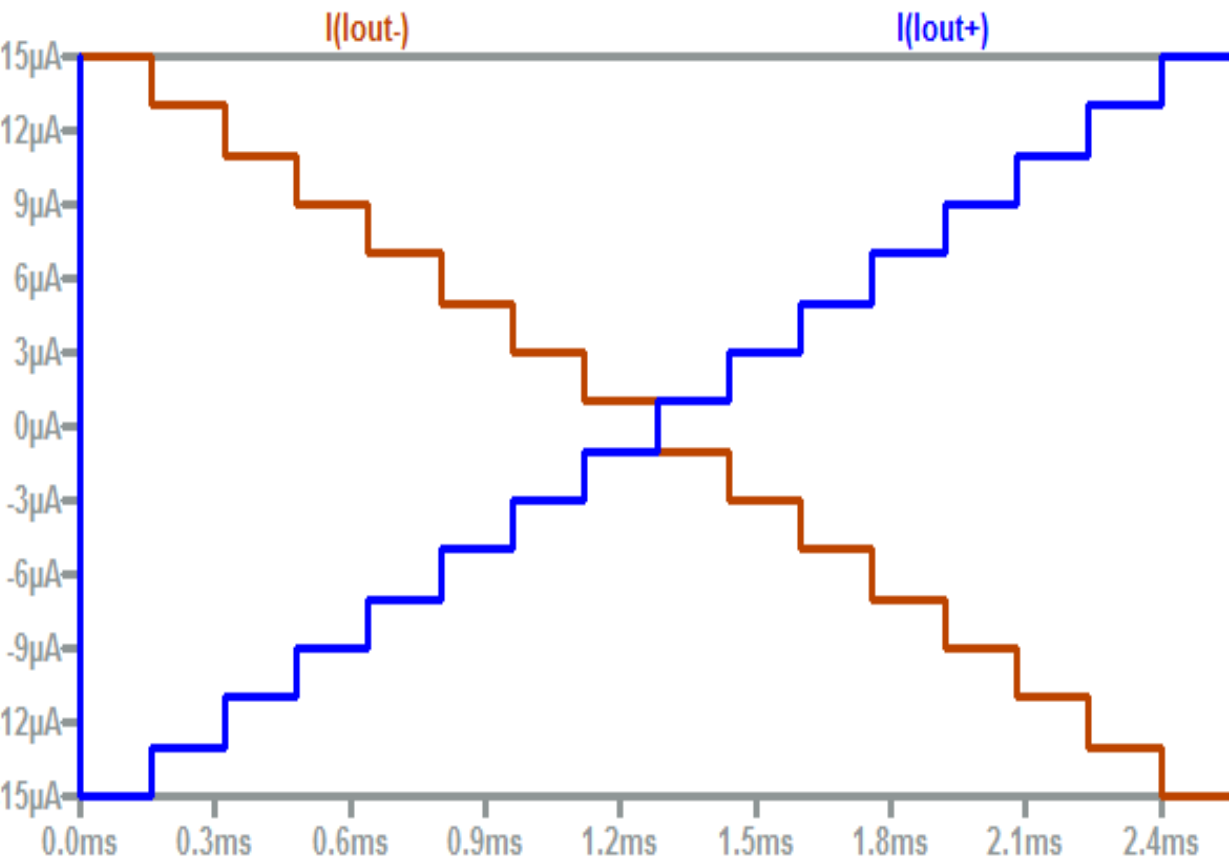
$$I_{out-} = I + 2I - 4I - 8I = -9I$$

$$I_{out+} = -I - 2I + 4I + 8I = 9I$$

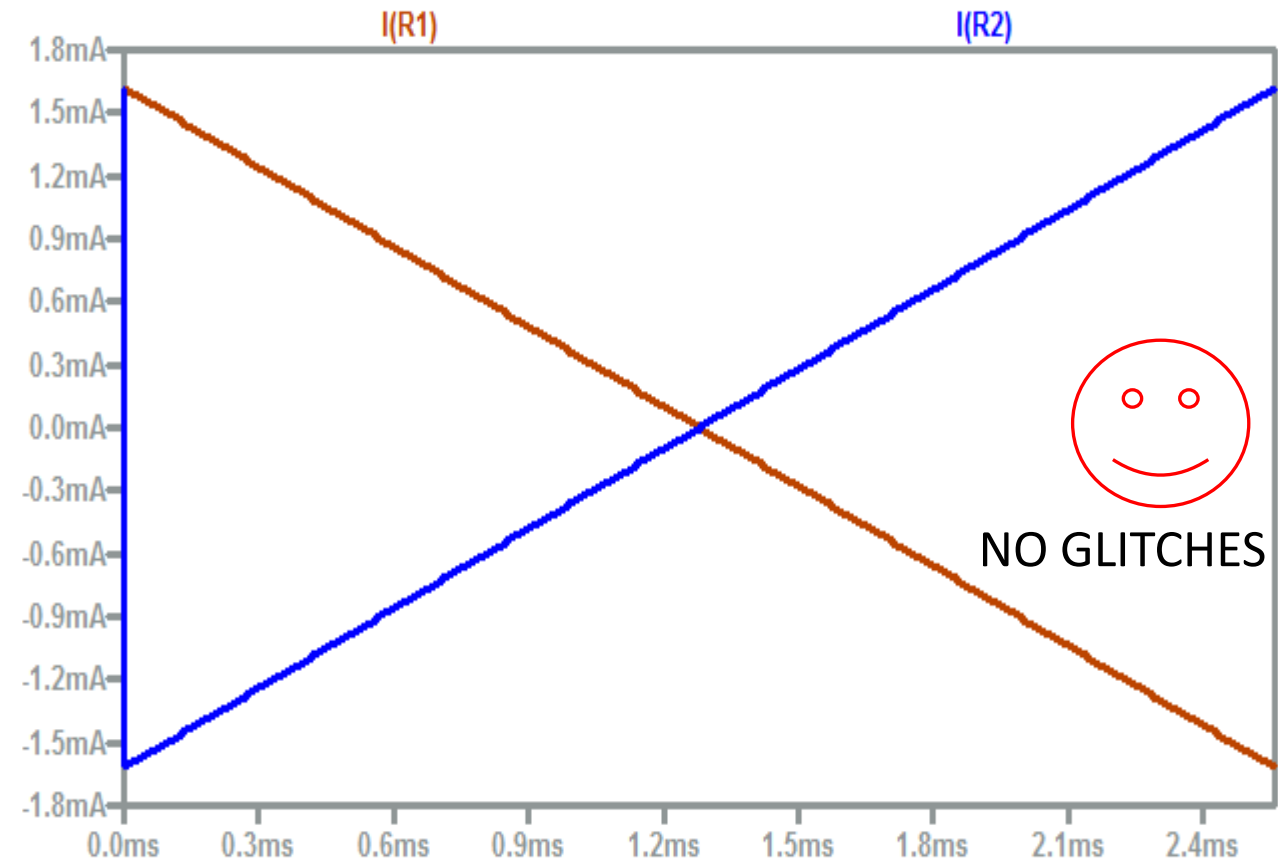


Current Steering Mode Gray Code Input DAC SPICE Simulation Results

4-bit case



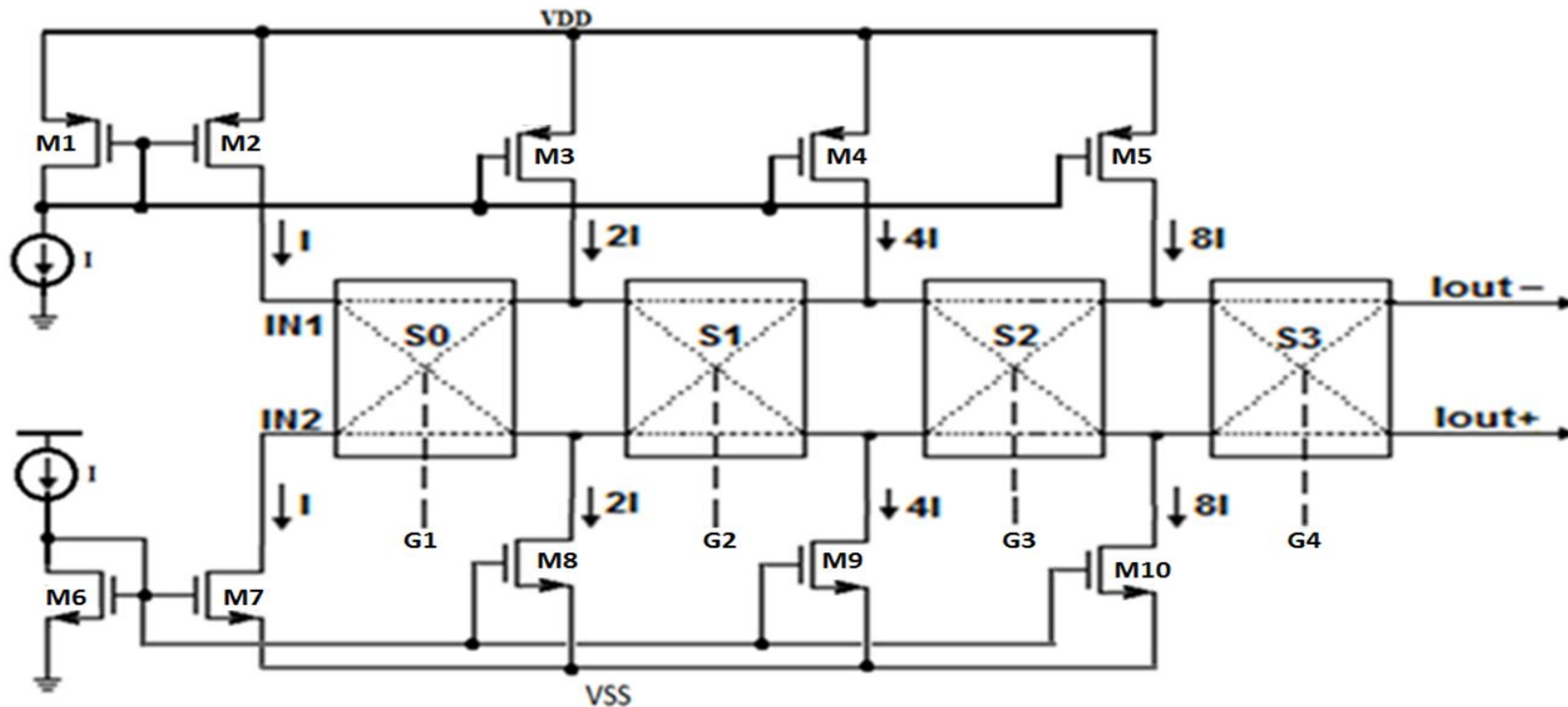
8-bit case



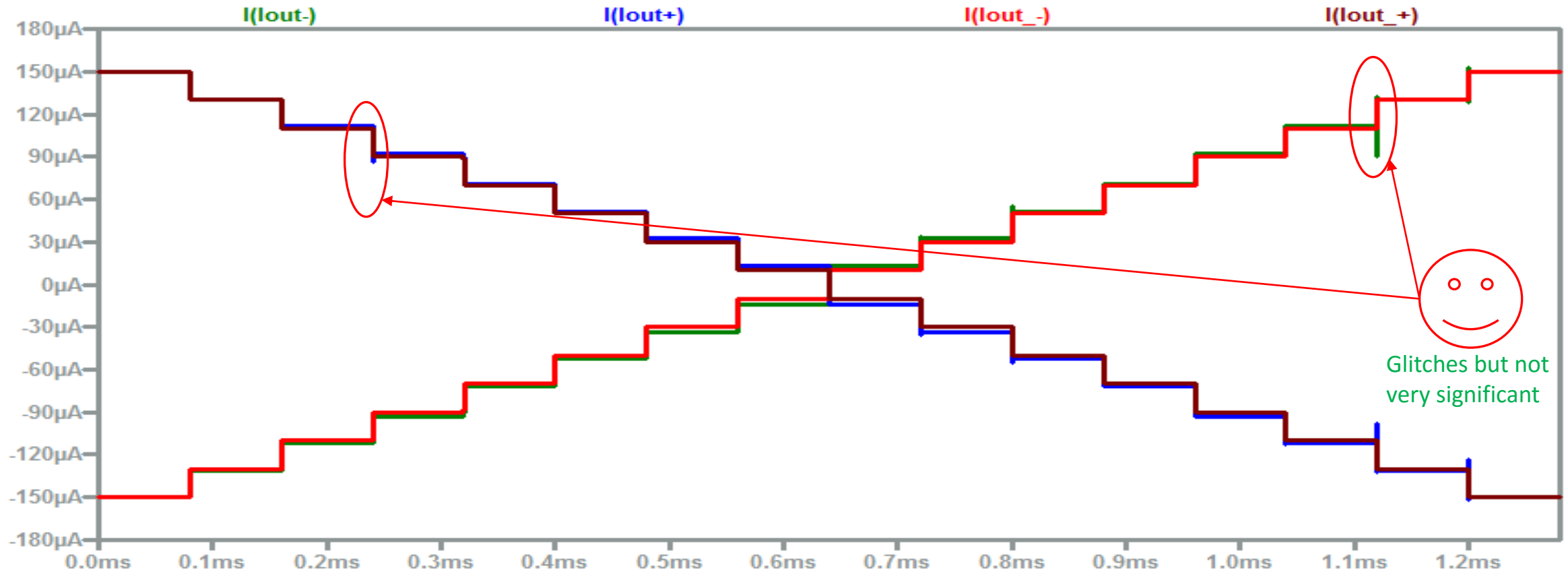
Current Steering Mode Gray Code Input DAC MOSFET Implementation

$M2, M3, M4, M5$ generate $I, 2I, 4I, 8I$ (current source)

$M7, M8, M9, M10$ generate $I, 2I, 4I, 8I$ (current sink)

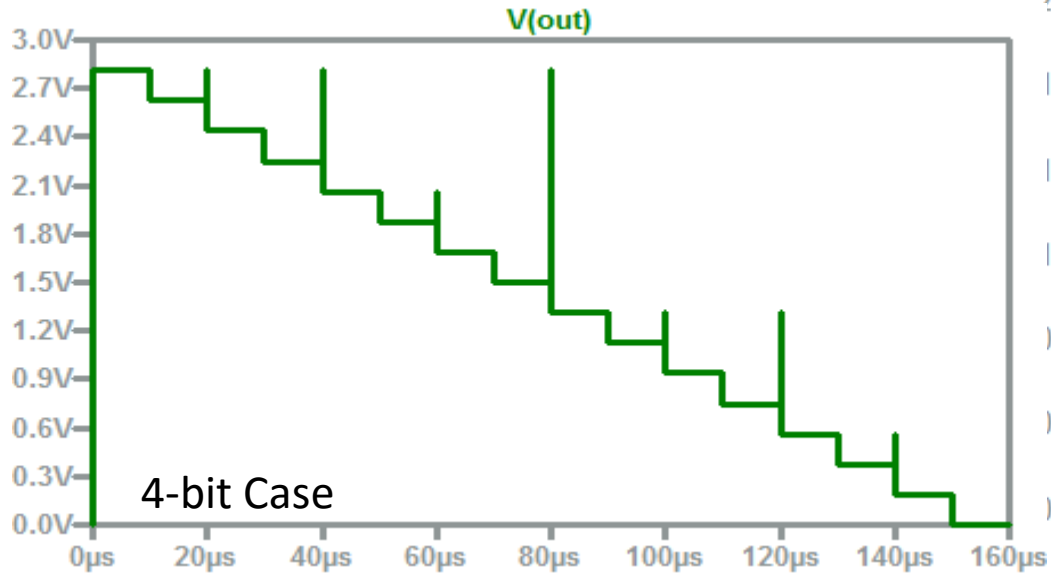
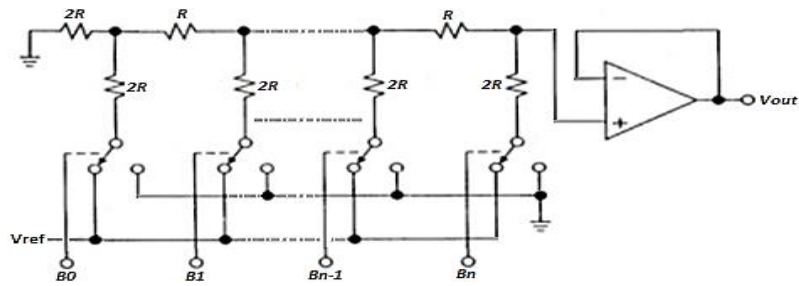


Current Steering Mode Gray Code Input DAC MOSFET Implementation Simulation Results



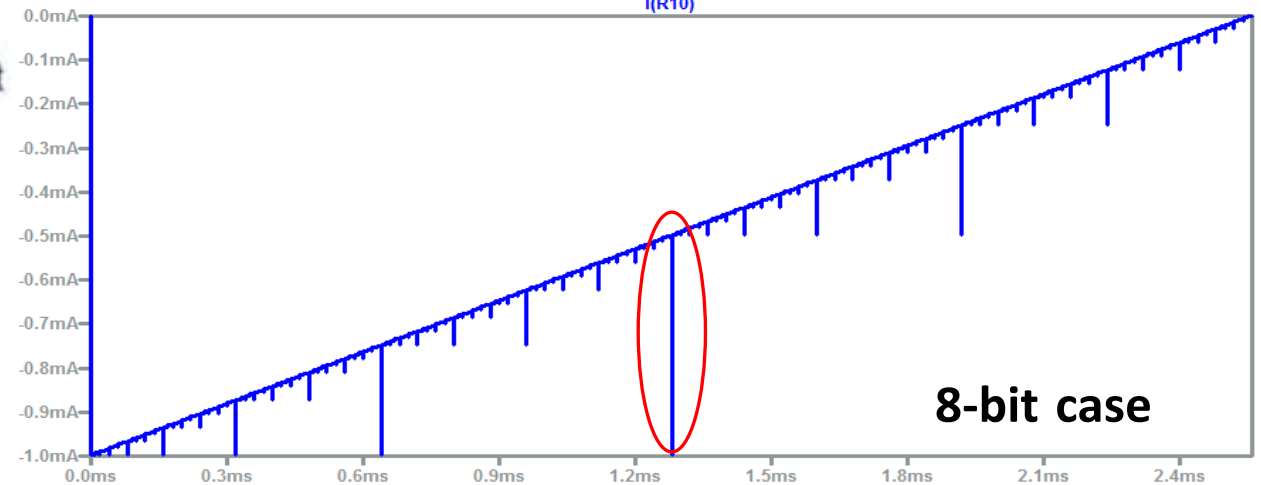
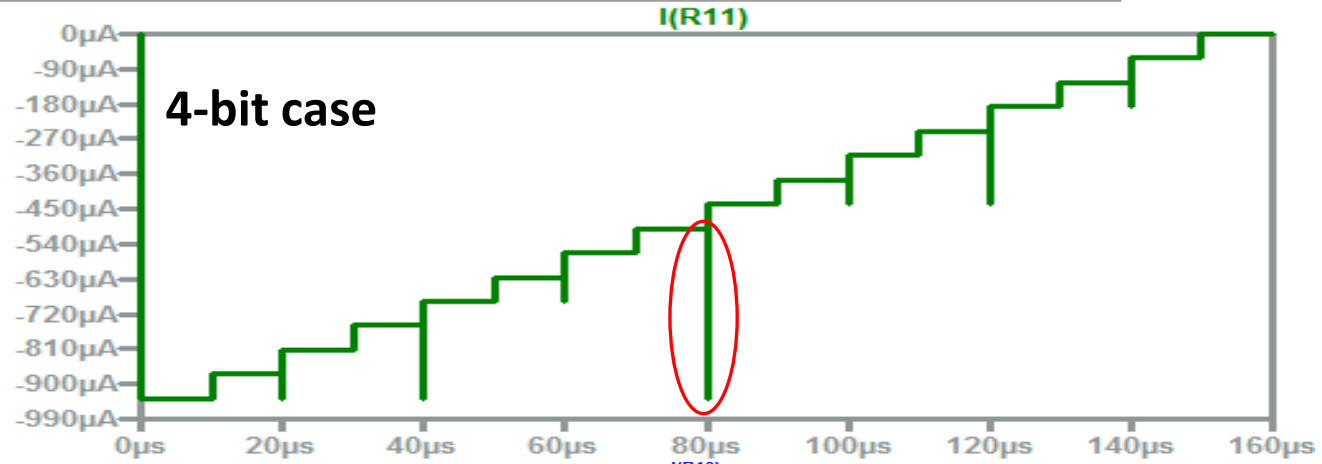
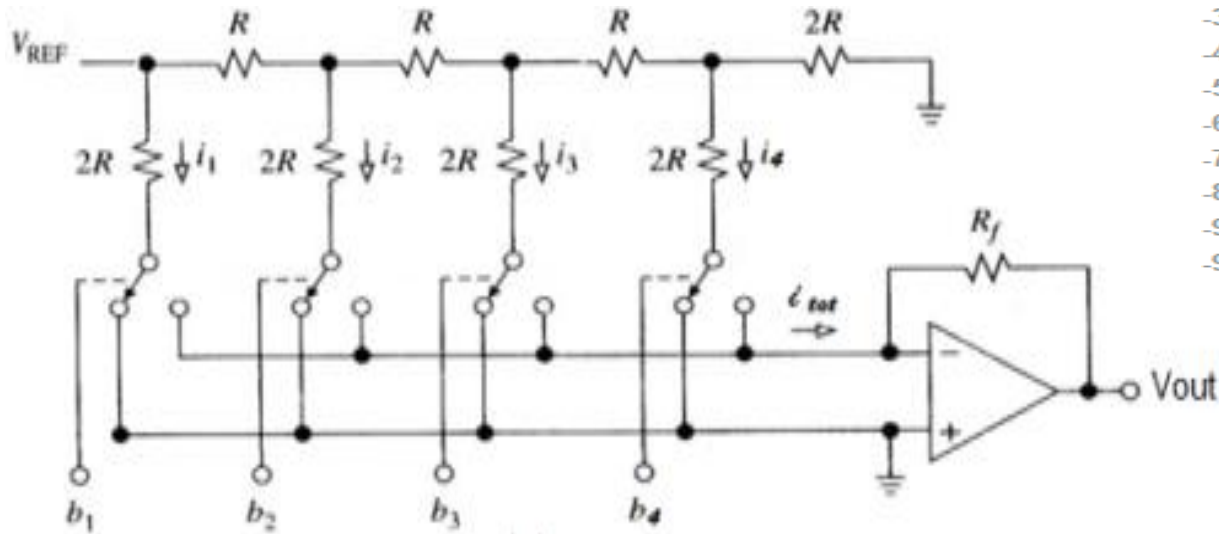
These glitches are due to mismatch of PMOS and NMOS

R-2R Binary Voltage Mode DAC



Glitches get introduced in binary code R-2R DAC

R-2R Binary Current Mode DAC



Conclusion

- ✓ R-2R DACs prone to glitches → Multiple bits switching at a time.
- ✓ Claims of Gray code DACs being difficult to design but successfully designed and simulated
 - ✓ Gray code Input DACs reduce glitches considerably
 - ✓ No extra space needed for IC
 - ✓ No extra circuit needed to remove glitches

Final Statement

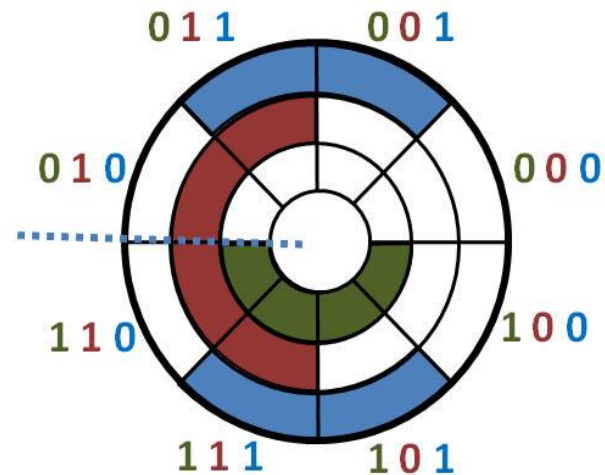
Coding method can lead to **robust** mixed-signal circuit design.

Gray code was invented by Frank Gray at Bell Lab in 1947.

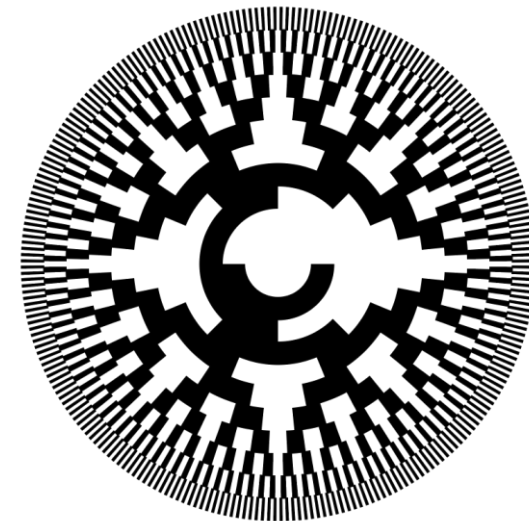
"Two-Way Television" - Booklet by AT&T-Bell Labs, April 1930



FRANK GRAY and A. L. Johnsrud in television booth. Behind the glass panels at sides and top are the photo-electric cells.



$Q_2Q_1Q_0$
000
001
011
010
110
111
101
100



Thank you